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Effect of Disbonds on the Fatigue Endurance of Composite Scarf Joints

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Abstract
The certification of scarf repairs requires that the repair is capable of handling flight loads in the presence of disbonds. This paper presents a study of the fatigue disbond growth behaviour of scarf joints. By determining the strain energy release rates of a disbond in a scarf joint subjected to a unit load, a predictive model based on linear elastic fracture mechanics is presented, which is shown to correlate well with experimental results. This method offers a promising technique for predicting the fatigue life of composite scarf joints with disbonds.

Introduction
A key airworthiness certification requirement for adhesively bonded scarf repairs of aircraft composite structures is to demonstrate through analysis or tests that catastrophic failure due to fatigue, environmental effects, manufacturing defects, or accidental damage will be avoided throughout the operational life of the aircraft [1]. While methods for predicting the residual strength of composite structures, without repairs [2] and with repairs [3, 4], are available in literature, there is a lack of analytical methods that can predict the growth rates of disbonds in scarf repairs. While the fatigue properties of a composite material can be determined using double cantilever beam (DCB) and end notched flexure (ENF) tests, it is not clear how the fatigue endurance of scarf repairs can be estimated. This paper aims to present a fracture mechanics based approach for predicting the disbond growth rate and fatigue life of scarf joints containing pre-existing flaws.

Theory
The growth rate of disbonds in composite structures under fatigue loading is commonly expressed in terms of the cyclic strain energy release rate, \( \Delta G = G_{\text{max}} - G_{\text{min}} \), where the parameters \( C \) and \( m \) depend on the material and the loading ratio (defined as the ratio between the minimum and the maximum load in a cycle, i.e. \( R = P_{\text{min}} / P_{\text{max}} \)).

\[
\frac{da}{dN} = C(\Delta G)^m
\]  

(1)

For a scarf joint containing an embedded disbond, it was found in previous literature [5], that the energy release rate for a given load, \( G_{\text{max}} \), at the crack tip can be determined using a reference stress method outlined below:

\[
G_{I,\text{max}} = \left(\frac{\sigma_0}{\sigma_{\text{ref}}}\right)^2 G_{I,\text{ref}}
\]

\[
G_{II,\text{max}} = \left(\frac{\sigma_0}{\sigma_{\text{ref}}}\right)^2 G_{II,\text{ref}}
\]  

(2)

where \( G_{I,\text{ref}} \) and \( G_{II,\text{ref}} \) are the mode I and mode II strain energy release rates when the scarf joint with a flaw of length \( a \) is subjected to a reference stress \( \sigma_{\text{ref}} \). Under mixed-mode loading, the two individual strain energy release rates can be combined to form a single correlating parameter using the Benzeggagh-Kenane (B-K) fracture criterion [6], which is given by
Alternatively the mode I and mode II strain energy release rates can be combined using the power law criterion,

\[ G_{\text{power-law,max}} = a \left( G_{I,max}^\eta + G_{II,max}^\eta \right)^{\frac{1}{\eta}} \]  

For this paper, a value of \( \eta = 1.75 \) was used in the B-K fracture criterion and a value of \( \alpha = 2 \) was used in the power law equation. These values were taken from literature [7] and were noted to provide fairly good predictions of the static strength of composite structures.

The number of fatigue cycles spent in growing a disbond from an initial length of \( a_0 \) to the final critical length \( a_c \), which is essentially the fatigue life, can be determined by integrating the reciprocal of Equation (1), yielding,

\[ N_f = \int_{a_0}^{a_c} \left( \frac{da}{dN} \right)^{-1} da \]  

The critical disbond length \( a_c \) can be determined from the unstable growth condition

\( \left( \frac{\sigma_{\text{max}}}{\sigma_{\text{ref}}} \right)^2 G_{\text{BK,ref}}(a_c) = G_{IC} \)

For a scarf joint containing a disbond of length \( a_0 \), the fatigue limit \( \sigma_{\text{FL}} \) and static residual strength \( \sigma_{\text{ULT}} \) can be estimated by

\[ \sigma_{\text{FL}} = \sigma_{\text{ref}} \left( \frac{\Delta G_{\text{th}}}{(1 - R^2) G_{\text{ref}}(a_0)} \right) \]

\[ \sigma_{\text{ULT}} = \sigma_{\text{ref}} \left( \frac{G_{IC}}{G_{\text{ref}}(a_0)} \right) \]

where \( G_{\text{ref}} \) denotes the reference strain energy release rate according to Equations (3) or (4), depending on the failure criterion. Therefore it is interesting to note that the ratio between the fatigue limit and static strength of a scarf joint is equal to the square root of the ratio between threshold and toughness,

\[ \frac{\sigma_{\text{FL}}}{\sigma_{\text{ULT}}} = \sqrt{\left( \frac{1 - R^2}{1 - R^2} \right) \frac{G_{IC}}{G_{IC}}} \]

which provides a rapid estimate of the fatigue limit from the static test, providing the initial flaw is large enough such as the linear elastic fracture mechanics approach is valid.

Experiments and results

Adhesively bonded composite scarf joints were first manufactured using VTM264/T700 [8] unidirectional carbon/epoxy composite prepreg with a ply thickness of 0.22 mm, a curing temperature of 120°C for 1 hour, and a lay-up of \([45^\circ/0^\circ/0^\circ/90^\circ/-45^\circ]_{2S}\). Cured laminates were machined to a 3° angle using a milling machine and then bonded with VTA260 adhesive at a curing temperature of 120°C for 1 hour. Inserts, with a length of 12 mm, were placed at the composite-adhesive interface at the feathered end of the scarf as an initial disbond.

The joints were loaded in static tension under conditions similar to that employed in reference [5] to determine the residual strength of the joint with a disbond length of 12 mm. It was observed that the fracture occurred in the composite adherend near the composite-adhesive interface [5], at a distance from the composite-adhesive interface comparable to a fibre diameter. The joint was observed to have an average static residual strength of 264 MPa. The joints were then tested in fatigue with a cyclic loading ratio \( (R) \) of 0.1, at a frequency of 10 Hz, and peak loads at 50%, 35%...
and 25% of the static residual strength. A travelling microscope was used to capture fracture propagation along the side of the scarf joint. The joints were loaded to failure at 50%, \(1 \times 10^5\) cycles at 35% and \(1 \times 10^6\) cycles at 25%.

Fatigue cracks in the scarf joints, at loads of 50% and 35% residual strength, were observed to first propagate across the adhesive, from one composite-adhesive interface to the other interface, and then continue travelling down the bondline similar to the static fracture path reported in [5], shown in Figure 1. At the peak load of 50% residual strength, the joint failed catastrophically after 24,658 cycles. At the peak load of 25% residual strength, no crack propagation was observed after \(1 \times 10^6\) cycles, suggesting that the applied peak loads were below the fatigue threshold strength of the joint.

For the composite material system employed in this study, the constants \(C\) and \(m\), in Equation (1) were determined from literature [9] under Mode I interlaminar DCB fatigue tests (\(C = 0.08\) and \(m = 4.5\)).

**Computational modelling**

Finite element models were developed in Abaqus 6.10 [10] for this analysis. Plane strain four-node orthogonal (CPE4) and three-node triangular (CPE3) elements were used to model the adhesive and the composite adherends, with ply-level mesh refinement. Material properties for the composite plies and the adhesive are listed in Table 1 and Table 2, respectively. The properties of +/- 45° plies were derived using ply coordinate transformation equations, considering only the terms in the plane of the model [11]. Boundary conditions were applied on both ends of the scarf joint to replicate experimental testing constraints, and consisted of constrained displacements in all degrees of freedom, except for the loading displacement at one end. A non-linear implicit numerical analysis was performed using Abaqus/Standard to account for the effects of secondary bending.

<table>
<thead>
<tr>
<th>E11 (GPa)</th>
<th>E22 = E33 (GPa)</th>
<th>ν12 = ν13</th>
<th>ν23</th>
<th>G12 = G13 (GPa)</th>
<th>G23 (GPa)</th>
</tr>
</thead>
<tbody>
<tr>
<td>120</td>
<td>7.5</td>
<td>0.32</td>
<td>0.33</td>
<td>3.9</td>
<td>2.3</td>
</tr>
</tbody>
</table>

Table 2: Material properties of VTA260 adhesive

<table>
<thead>
<tr>
<th>E (GPa)</th>
<th>ν</th>
<th>G (GPa)</th>
</tr>
</thead>
<tbody>
<tr>
<td>3</td>
<td>0.35</td>
<td>1.1</td>
</tr>
</tbody>
</table>

Based on the fractographic observations described in the previous section that the fracture occurred in the composite at a small distance comparable to a fibre diameter away from the composite-adhesive interface, the onset and propagation of cracks was assumed to be within the composite, adjacent to the composite-adhesive interface. The effect of the extremely thin layer of resin-fibre material is ignored for simplicity; the crack path was assumed to be along the adherend-adhesive interface. With reference to Figure 2, interface 1 represents disbonds and crack paths propagating between the feathered end of a scarfed adherend and the adhesive. Interface 2 represents disbonds and crack paths between the blunt end of the scarfed adherend and the adhesive. The distance (\(\Delta a\)) between the nodes along the bondline was refined to approximately 0.264 mm. Using the virtual crack closure technique (VCCT), the strain energy release rates (\(G_I\) and \(G_{II}\)) were determined. The results are displayed in Figure 3 for a range of flaw sizes (\(a\)), normalised by the length of the scarf (\(L\)), under an applied load of 1.0 MPa. From these results, the appropriate strain energy release rates at any given applied load and crack length can be readily computed from Equation (2).
Comparison between numerical predictions and experimental data

Numerical predictions were obtained from Interface 2 as shown in Figure 2. Figure 4 shows the effect of mixed-mode criterion on fatigue crack growth loaded at 35% and 50% of the residual joint strength. At 35% residual strength, both criteria appear to correlate fairly well to experimental data. The B-K criterion is observed to perform better than the power-law with $\alpha = 2$. At 50% residual strength, the B-K criterion is observed to predict the life of the joint more accurately than the power law. It should be noted that both criteria provided conservative predictions by over-predicting the length of the crack. Overall, this shows that the B-K criterion is capable of accurately predicting the fatigue crack growth behaviour and the life of the composite scarf joints under fatigue loading conditions.

Finally, Figure 5 shows numerical predictions on the life of the joint with an embedded disbond of 12 mm at various maximum fatigue loads in the form S-N curve. A reasonable correlation between experimental data and model predictions can be observed. The S-N curve correctly predicted that the life of the joint at 25% of the residual strength was higher than $1 \times 10^6$ cycles.

Conclusion

This paper presents a linear elastic fracture mechanics-based methodology for predicting the fatigue life of adhesively bonded composite scarf joints with disbonds. The fracture behaviour and crack path were determined through microscopy. By applying the VCCT along the observed crack path and determining the strain energy release rates at unit loads, the fatigue crack growth rate and life of scarf joints can be accurately predicted.

Figure 1: (a) Overall crack propagation in the fatigued scarf joint. (b) Typical crack propagation path near ply terminations. One quarter of the laminate stack shown.

Figure 2: Critical regions of the scarf joint embedded with the VCCT model. Two different numerical models were generated.
Figure 3: Numerically derived Mode I and II strain energy release rate ($G_I$ and $G_{II}$) curves of the scarf joint, under unit load (1MPa), at a range of flaw sizes ($a$), normalised by the length of the scarf ($L$).

Figure 4: Effect of mixed mode criterion on fatigue crack growth loaded at a) 35% and b) 50% of the residual joint strength. (Power Law, $\alpha = 2$; B-K, $\eta = 1.75$)
Figure 5: S-N curve of numerical predictions against experimental results.

References